

# LEAP

## A Tool for the Parametrized Verification of Concurrent Datatypes

Alejandro Sánchez<sup>1</sup>

César Sánchez<sup>1,2</sup>

<sup>1</sup>IMDEA Software Institute, Spain

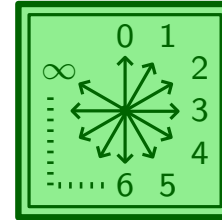
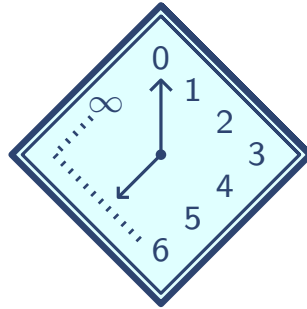
<sup>2</sup>Institute for Information Security (CSIC), Spain

CAV'14, Vienna, 21 July 2014

# LEAP: Objectives

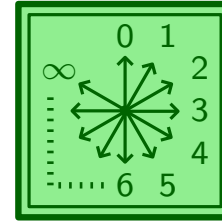
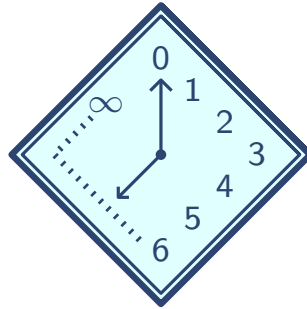
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## Temporal Properties

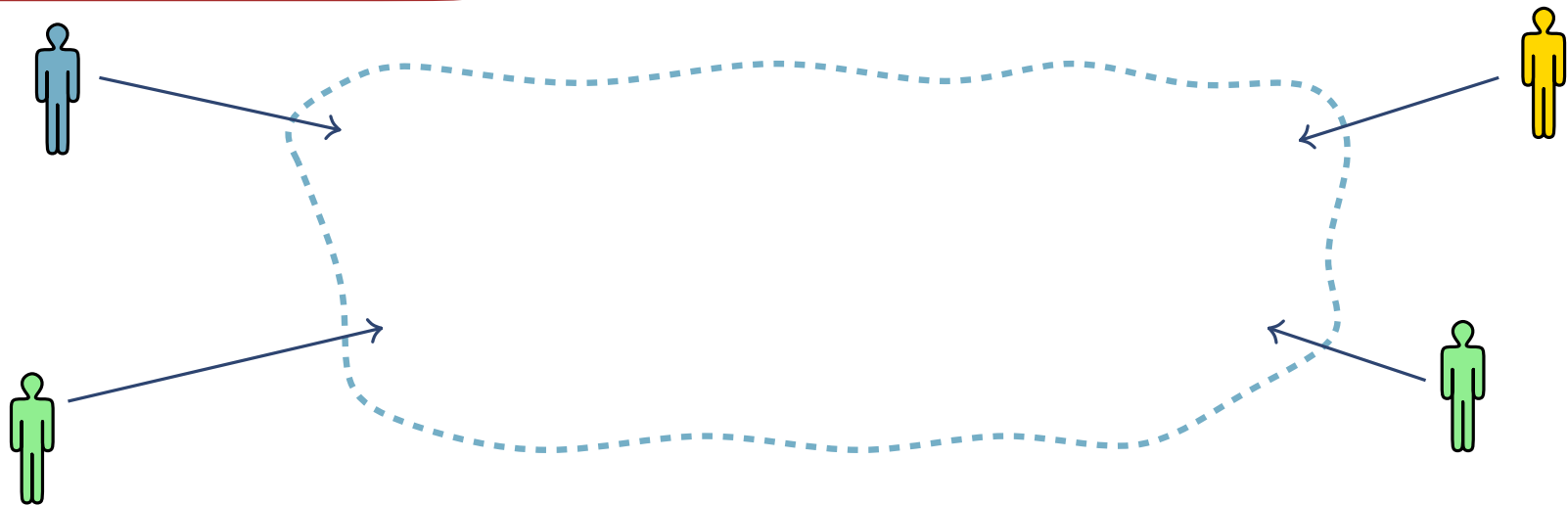


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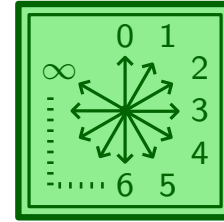
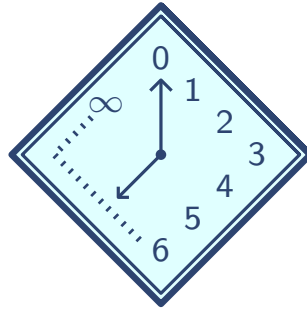


## Concurrent Datatypes

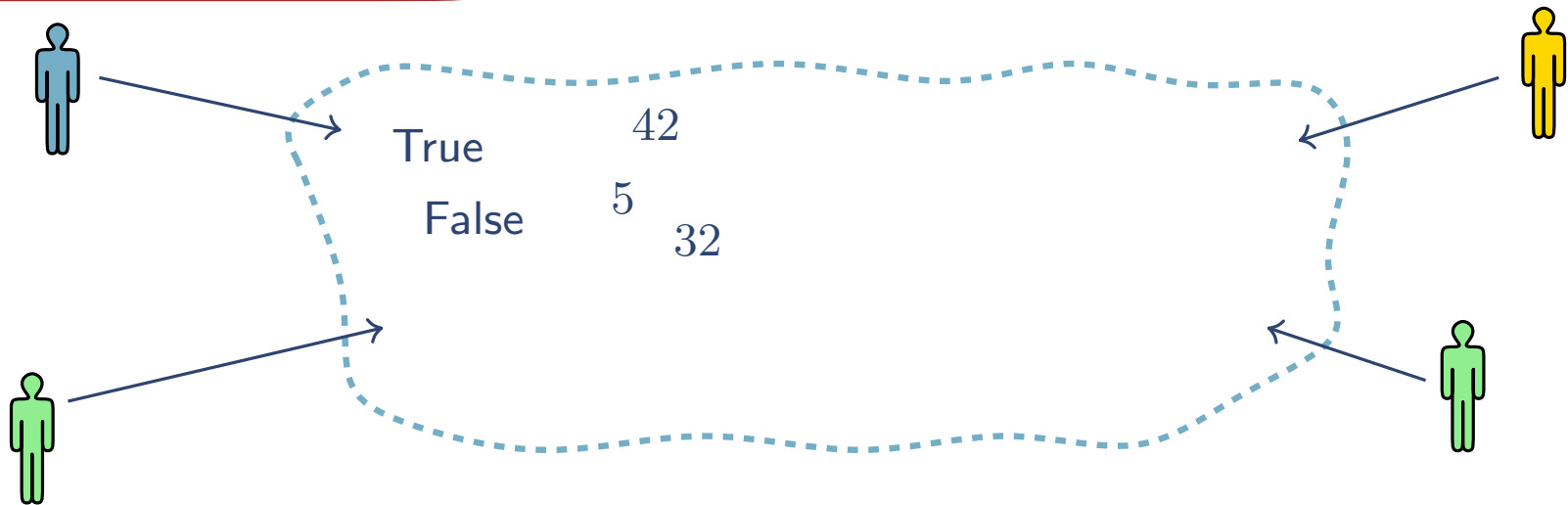


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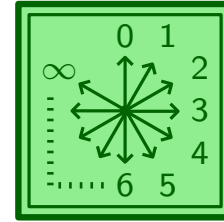
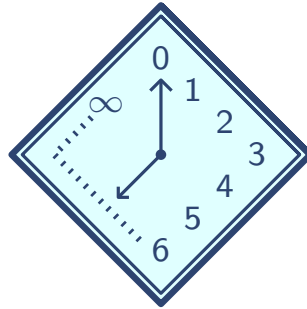


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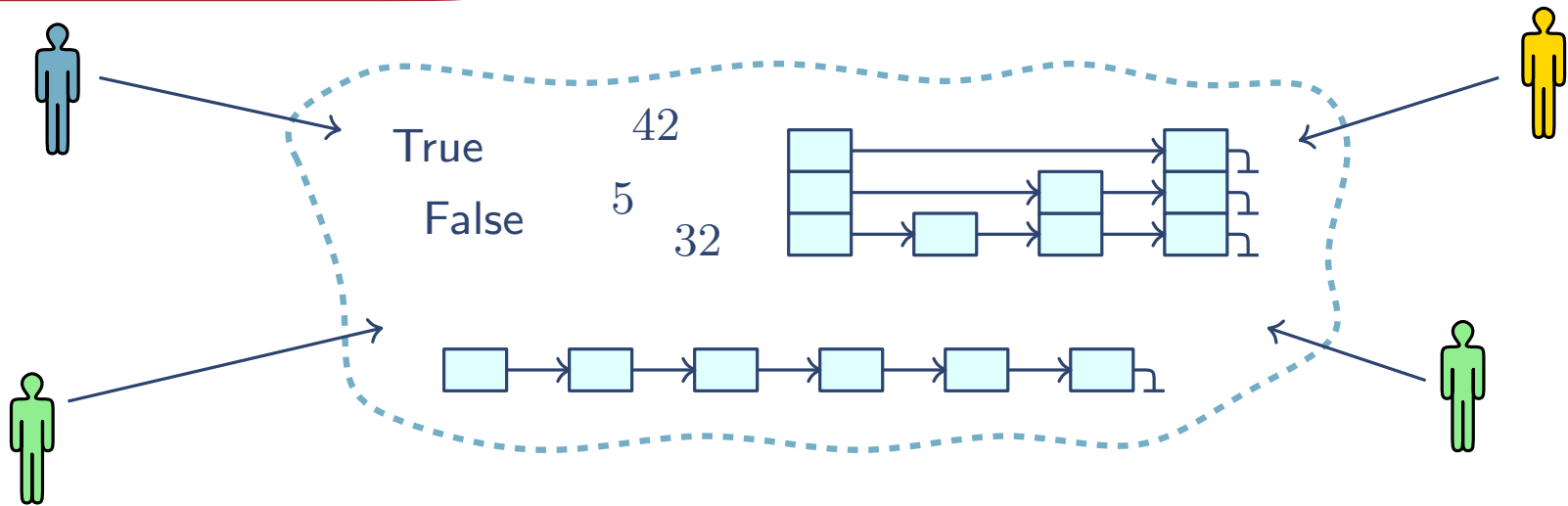


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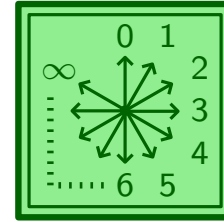
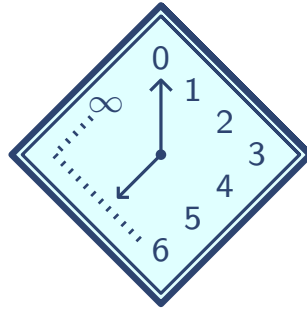


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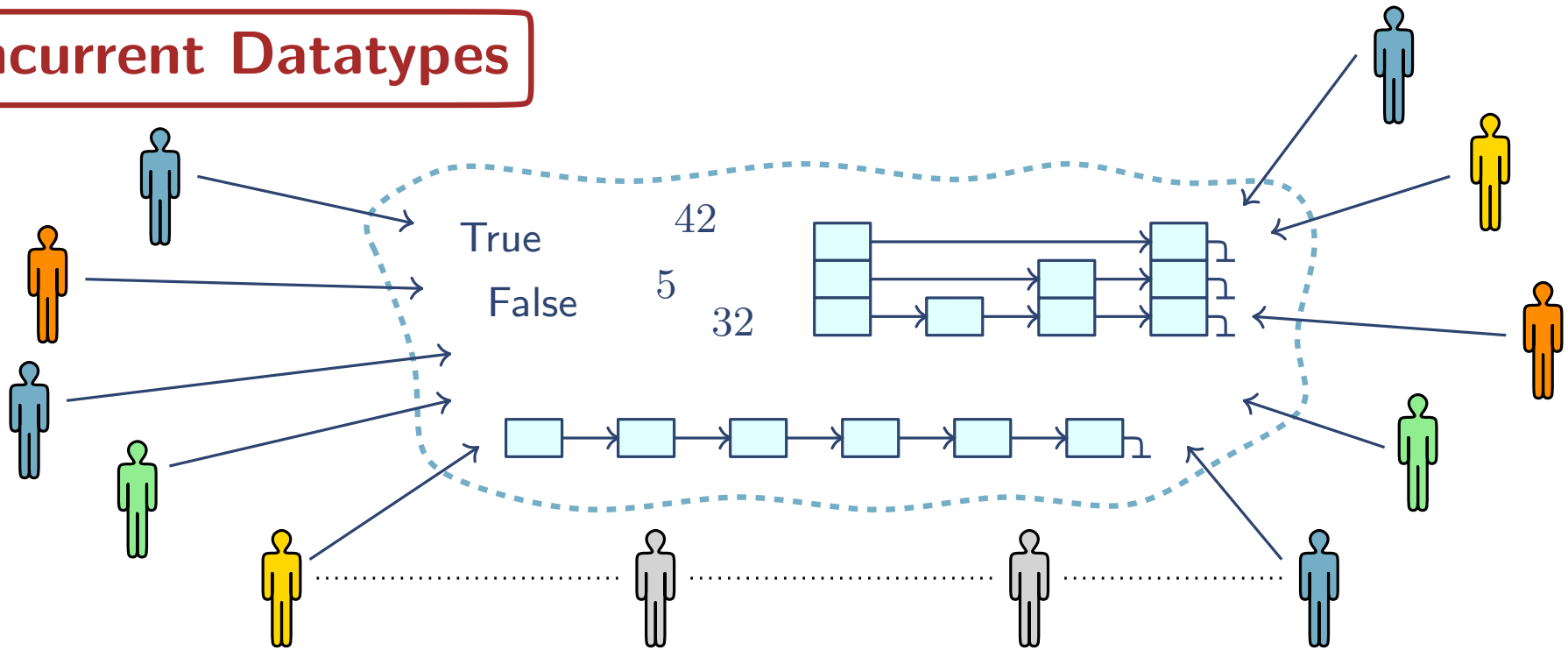


# LEAP: Objectives

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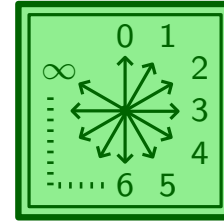
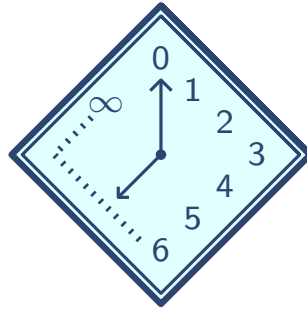
## Concurrent Datatypes



## Parametrized Verification

# LEAP: Objectives

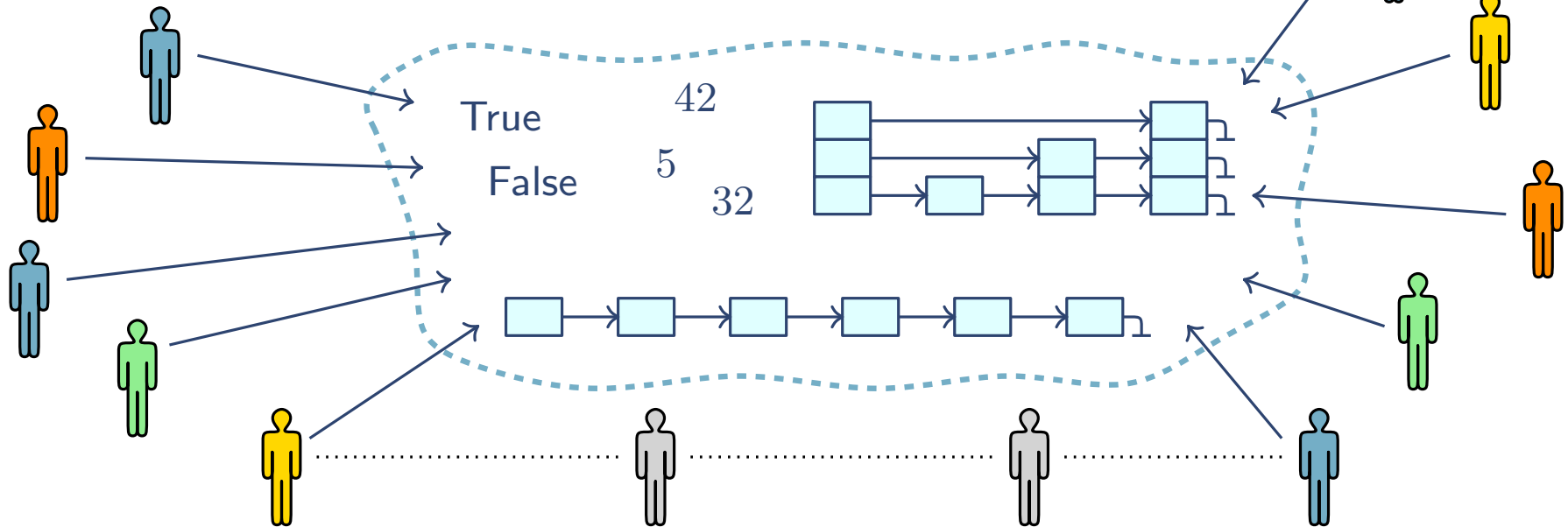
Temporal Properties



Deductive methods  
+  
Decision procedures



Concurrent Datatypes



Parametrized Verification



# LEAP: Description

- ▶ **Deductive** theorem prover
- ▶ Aims verification of **temporal properties**
- ▶ Designed to verify **concurrent datatypes**
- ▶ Specific for **parametrized systems**
- ▶ Automation based on **decision procedures**
- ▶ Built on top of state-of-the-art **SMT solvers**
- ▶ Targets both **safety** and **liveness** verification

# LEAP: Structure



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Program



```
global
  addr head, tail; ghost addrSet region;
procedure insert (e:elem)
  addr prev, curr, aux;
begin
1: prev := head;
2: prev->lock;
3: curr := prev->next;
4: curr->lock;
5: while curr->data < e do
    .....
11: end while
12: if curr != null /\curr->data > e then
13:   aux := malloc(e,null,#);
14:   aux->next := curr;
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Conditionals, loops

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Atomic sections



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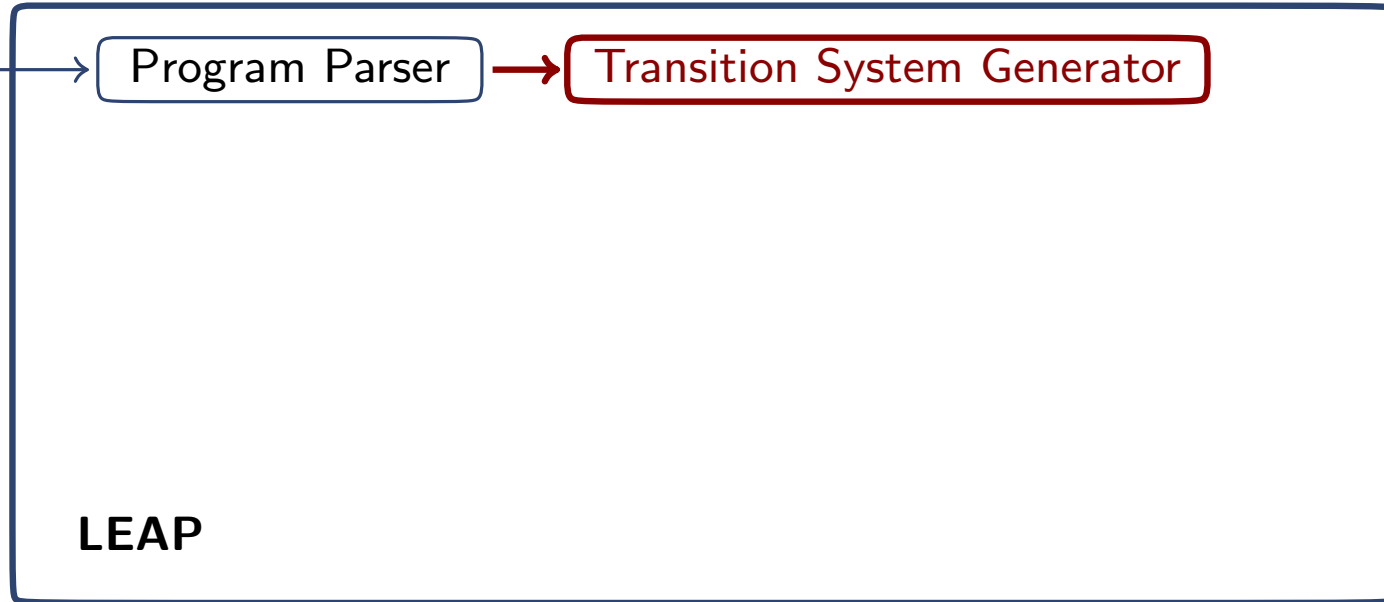
Atomic sections

Ghost code


Location labeling

# LEAP: Structure

Program

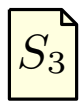
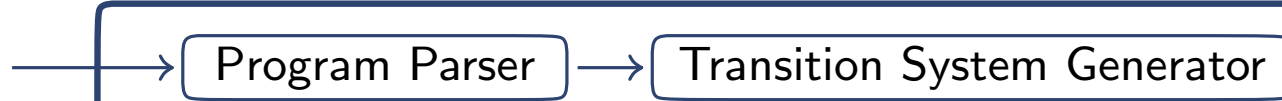


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$$S[N] = T_1 \parallel T_2 \parallel \cdots \parallel T_N$$


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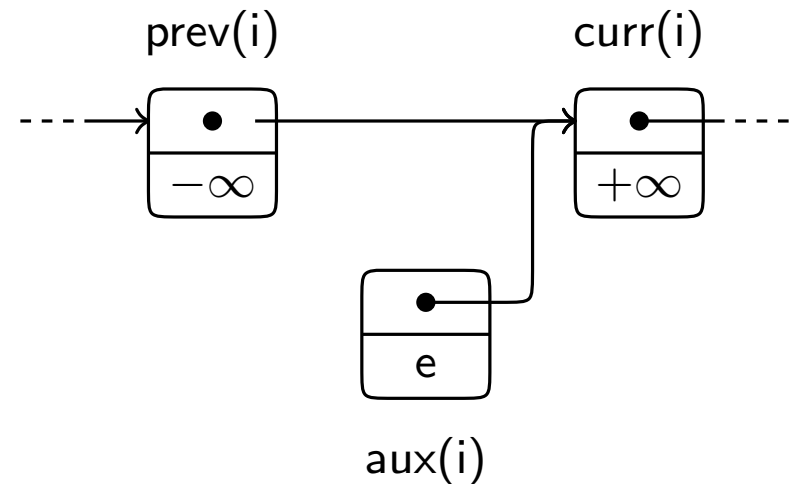
Program



**LEAP**

Specs

```
vars: tid i
specification [aux_ready] :
  @connect(i). ->
    (rd(heap, prev(i)).data < e      /\
     rd(heap, curr(i)).data > e      /\
     rd(heap, aux(i) ).data = e      /\
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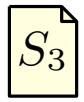
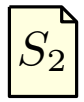
Program



Program Parser



Transition System Generator

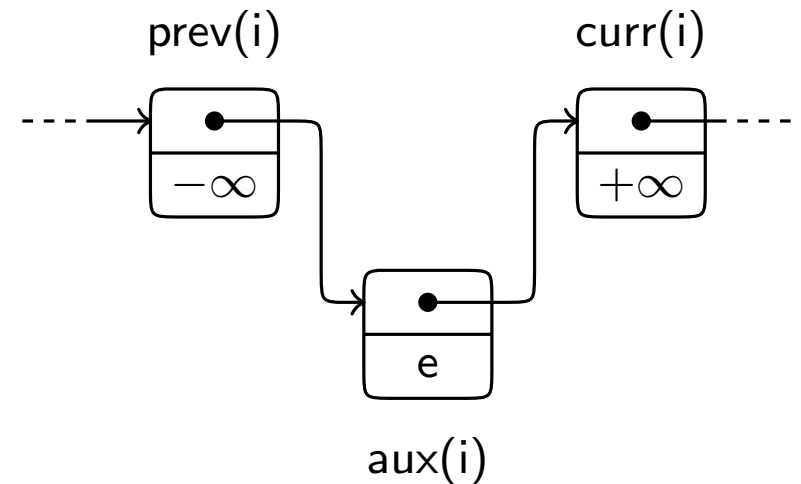


Formula Parser

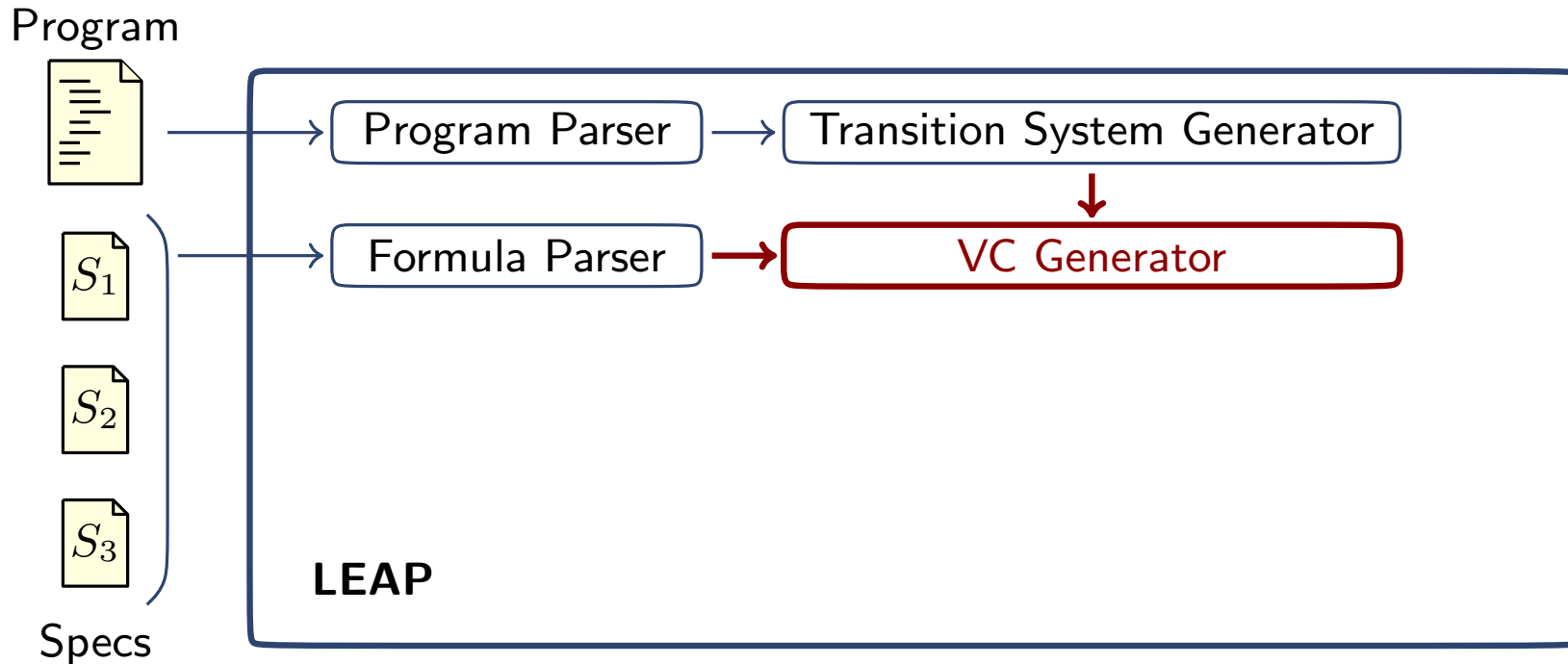
**LEAP**

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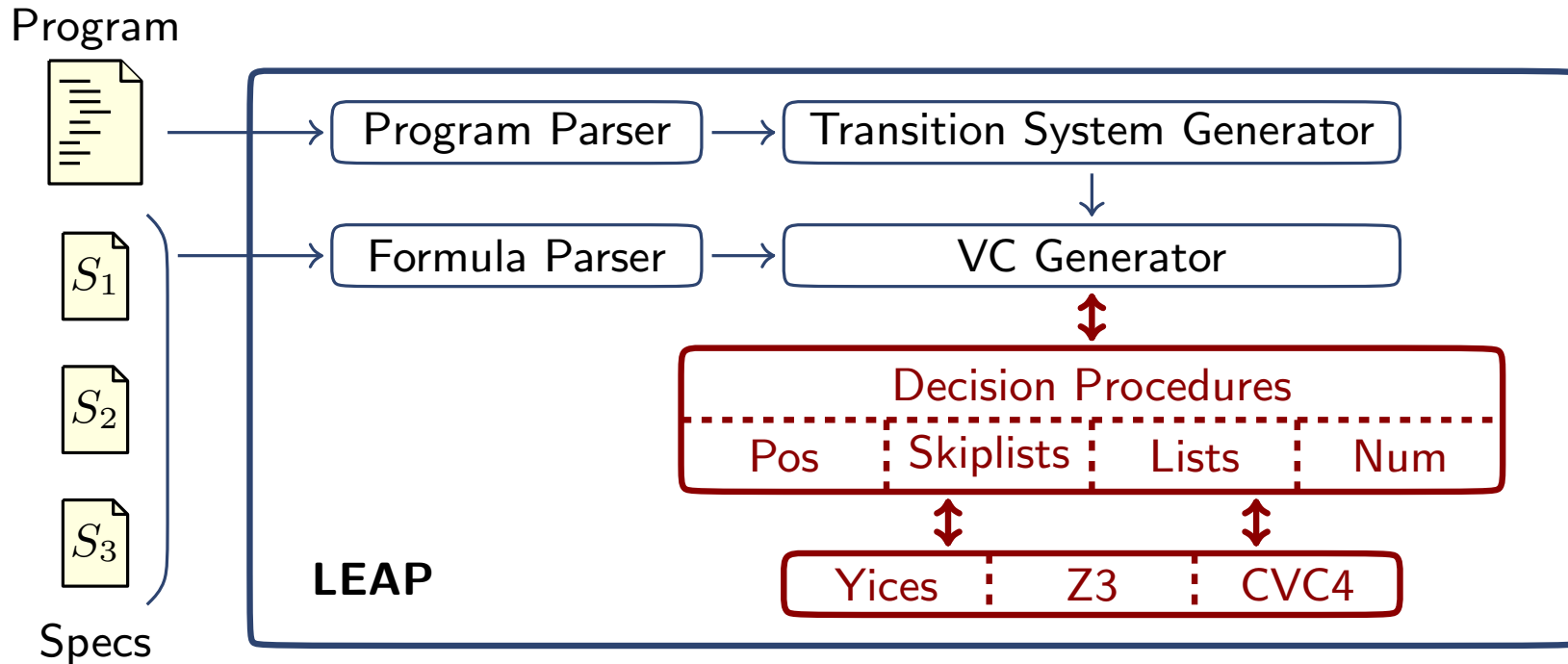


Each **VC** represents a **small-step** in the execution

All VC are **QF** as long as specs are QF

LEAP supports **heuristics and tactics** to aid verification

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All VC are **QF** as long as specs are QF

LEAP supports **heuristics and tactics** to aid verification

Check validity using **specialized decision procedures**

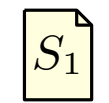
# LEAP: Structure

Program



Program Parser

Transition System Generator



Formula Parser

VC Generator



LEAP

Decision Procedures

Pos

Skiplists

Lists

Num

Yices

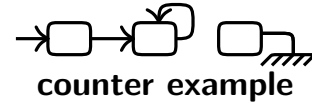
Z3

CVC4

VC1 ✓

VC2 ✓

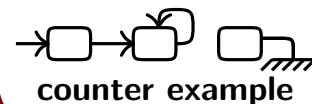
VC3 ✗



counter example

VC4 ✓

VC5 ✗



counter example

Specs

All VCs are checked **valid**?



Specification is verified

Generate small counter examples to aid the programmer



# LEAP: Current Status

- ▶ **Full** implementation for **safety** properties
- ▶ **Ongoing** implementation for **liveness** properties [TIME'14]
- ▶ **Specialized decision procedures** for:
  - ▶ Presburger arithmetic with sets
  - ▶ Concurrent fine-grained and lock-free lists [ICFEM'10]
  - ▶ Concurrent fine-grained bounded height skiplists [NFM'11]
  - ▶ Unbounded skiplists [ATVA'14]
- ▶ We have **verified** structural and functional specifications of:
  - ▶ Mutual exclusion protocols based on integers and sets
  - ▶ Concurrent lock-coupling single-linked lists
  - ▶ Lock-free queues and stacks
  - ▶ Bounded and unbounded skiplists

# LEAP: Experimental Results

	formula	#solved vc		Brute time(s.)	Heurist. time(s.)	DP time(s.)		LEAP time(s.)		
		idx	#vc			pos	dp		slowest	average
1	list	0	61	38	23	$\infty$	18.67	11.90	0.30	0.20
2	order	1	121	62	59	998.35	1.12	0.03	0.01	0.47
3	lock	1	121	76	45	778.15	0.47	0.02	0.01	0.18
4	next	1	121	60	61	$\infty$	2.11	0.61	0.01	0.59
5	region	1	121	95	26	$\infty$	22.58	18.17	0.18	0.23
6	disj	2	181	177	4	121.74	0.19	0.01	0.01	0.12
7	funSchLinear	1	121	97	24	$\infty$	6.29	3.04	0.05	0.08
8	funSchInsert	1	121	93	28	$\infty$	4.15	1.91	0.03	0.08
9	funSchRemove	1	121	93	28	$\infty$	5.40	2.60	0.04	0.10
10	funSearch	1	208	198	10	$\infty$	3.54	1.57	0.01	0.34
11	funInsert	1	208	200	8	$\infty$	0.50	0.01	0.01	0.22
12	funRemove	1	208	200	8	$\infty$	1.41	0.95	0.01	0.24
13	skiplist <sub>3</sub>	0	154	92	62	$\infty$	1221.97	776.45	15.27	0.45
14	region <sub>3</sub>	0	124	97	27	$\infty$	27.50	17.36	0.34	0.58
15	next <sub>3</sub>	0	84	65	19	$\infty$	0.67	0.09	0.01	0.20
16	order <sub>3</sub>	0	84	59	25	$\infty$	9.66	7.80	0.10	1.31
17	skiplist	0	560	532	28	$\infty$	19.79	5.40	0.24	0.15
18	region	0	1583	1527	56	$\infty$	44.28	22.66	0.54	1.35
19	next	0	1899	1869	30	$\infty$	3.19	0.32	0.02	1.59
20	order	0	2531	2474	57	$\infty$	11.19	2.35	0.84	6.75
21	mutex	2	28	26	2	0.32	0.01	0.01	0.01	0.01
22	minticket	1	19	18	1	0.04	0.01	0.01	0.01	0.01
23	notsame	2	28	26	2	0.13	0.03	0.01	0.01	0.01
24	mutexS	2	28	26	2	0.44	0.04	0.01	0.01	0.01
25	minticketS	1	19	18	1	0.31	0.01	0.01	0.01	0.01
26	notsameS	2	28	26	2	0.14	0.02	0.01	0.01	0.01

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13	skiplist <sub>3</sub>	0	154	92	62	$\infty$	1221.97	776.45	15.27	0.45
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12	funRemove	1	208	200	8	$\infty$	1.41	0.95	0.01	0.24
13	skiplist <sub>3</sub>	0	154	92	62	$\infty$	1221.97	776.45	15.27	0.45
14	region <sub>3</sub>	0	124	97	27	$\infty$	27.50	17.36	0.34	0.58
15	next <sub>3</sub>	0	84	65	19	$\infty$	0.67	0.09	0.01	0.20
16	order <sub>3</sub>	0	84	59	25	$\infty$	9.66	7.80	0.10	1.31
17	skiplist	0	560	532	28	$\infty$	19.79	5.40	0.24	0.15
18	region	0	1583	1527	56	$\infty$	44.28	22.66	0.54	1.35
19	next	0	1899	1869	30	$\infty$	3.19	0.32	0.02	1.59
20	order	0	2531	2474	57	$\infty$	11.19	2.35	0.84	6.75
21	mutex	2	28	26	2	0.32	0.01	0.01	0.01	0.01
22	minticket	1	19	18	1	0.04	0.01	0.01	0.01	0.01
23	notsame	2	28	26	2	0.13	0.03	0.01	0.01	0.01
24	mutexS	2	28	26	2	0.44	0.04	0.01	0.01	0.01
25	minticketS	1	19	18	1	0.31	0.01	0.01	0.01	0.01
26	notsameS	2	28	26	2	0.14	0.02	0.01	0.01	0.01

# LEAP: Experimental Results

	formula	#solved vc		Brute time(s.)	Heurist. time(s.)	DP time(s.)		LEAP time(s.)		
		idx	#vc			pos	dp		slowest	average
1	list	0	61	38	23	$\infty$	18.67	11.90	0.30	0.20
2	order	1	121	62	59	998.35	1.12	0.03	0.01	0.47
3	lock	1	121	76	45	778.15	0.47	0.02	0.01	0.18
4	next	1	121	60	61	$\infty$	2.11	0.61	0.01	0.59
5	region	1	121	95	26	$\infty$	22.58	18.17	0.18	0.23
6	disj	2	181	177	4	121.74	0.19	0.01	0.01	0.12
7	funSchLinear	1	121	97	24	$\infty$	6.29	3.04	0.05	0.08
8	funSchInsert	1	121	93	28	$\infty$	4.15	1.91	0.03	0.08
9	funSchRemove	1	121	93	28	$\infty$	5.40	2.60	0.04	0.10
10	funSearch	1	208	198	10	$\infty$	3.54	1.57	0.01	0.34
11	funInsert	1	208	200	8	$\infty$	0.50	0.01	0.01	0.22
12	funRemove	1	208	200	8	$\infty$	1.41	0.95	0.01	0.24
13	skiplist <sub>3</sub>	0	154	92	62	$\infty$	1221.97	776.45	15.27	0.45
14	region <sub>3</sub>	0	124	97	27	$\infty$	27.50	17.36	0.34	0.58
15	next <sub>3</sub>	0	84	65	19	$\infty$	0.67	0.09	0.01	0.20
16	order <sub>3</sub>	0	84	59	25	$\infty$	9.66	7.80	0.10	1.31
17	skiplist	0	560	532	28	$\infty$	19.79	5.40	0.24	0.15
18	region	0	1583	1527	56	$\infty$	44.28	22.66	0.54	1.35
19	next	0	1899	1869	30	$\infty$	3.19	0.32	0.02	1.59
20	order	0	2531	2474	57	$\infty$	11.19	2.35	0.84	6.75
21	mutex	2	28	26	2	0.32	0.01	0.01	0.01	0.01
22	minticket	1	19	18	1	0.04	0.01	0.01	0.01	0.01
23	notsame	2	28	26	2	0.13	0.03	0.01	0.01	0.01
24	mutexS	2	28	26	2	0.44	0.04	0.01	0.01	0.01
25	minticketS	1	19	18	1	0.31	0.01	0.01	0.01	0.01
26	notsameS	2	28	26	2	0.14	0.02	0.01	0.01	0.01

# LEAP: Experimental Results

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3	lock	1	121	76	45	778.15	0.47	0.02	0.01	0.18
4	next	1	121	60	61	$\infty$	2.11	0.61	0.01	0.59
5	region	1	121	95	26	$\infty$	22.58	18.17	0.18	0.23
6	disj	2	181	177	4	121.74	0.19	0.01	0.01	0.12
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13	skiplist <sub>3</sub>	0	154	92	62	$\infty$	1221.97	776.45	15.27	0.45
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16	order <sub>3</sub>	0	84	59	25	$\infty$	9.66	7.80	0.10	1.31
17	skiplist	0	560	532	28	$\infty$	19.79	5.40	0.24	0.15
18	region	0	1583	1527	56	$\infty$	44.28	22.66	0.54	1.35
19	next	0	1899	1869	30	$\infty$	3.19	0.32	0.02	1.59
20	order	0	2531	2474	57	$\infty$	11.19	2.35	0.84	6.75
21	mutex	2	28	26	2	0.32	0.01	0.01	0.01	0.01
22	minticket	1	19	18	1	0.04	0.01	0.01	0.01	0.01
23	notsame	2	28	26	2	0.13	0.03	0.01	0.01	0.01
24	mutexS	2	28	26	2	0.44	0.04	0.01	0.01	0.01
25	minticketS	1	19	18	1	0.31	0.01	0.01	0.01	0.01
26	notsameS	2	28	26	2	0.14	0.02	0.01	0.01	0.01

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3	lock	1	121	76	45	778.15	0.47	0.02	0.01	0.18
4	next	1	121	60	61	$\infty$	2.11	0.61	0.01	0.59
5	region	1	121	95	26	$\infty$	22.58	18.17	0.18	0.23
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13	skiplist <sub>3</sub>	0				$\infty$	1221.97	776.45	15.27	0.45
14	region <sub>3</sub>	0				$\infty$	27.50	17.36	0.34	0.58
15	next <sub>3</sub>	0				$\infty$	0.67	0.09	0.01	0.20
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18	region	0	1583	1527	56	$\infty$	44.28	22.66	0.54	1.35
19	next	0	1899	1869	30	$\infty$	3.19	0.32	0.02	1.59
20	order	0	2531	2474	57	$\infty$	11.19	2.35	0.84	6.75
21	mutex	2	28	26	2	0.32	0.01	0.01	0.01	0.01
22	minticket	1	19	18	1	0.04	0.01	0.01	0.01	0.01
23	notsame	2	28	26	2	0.13	0.03	0.01	0.01	0.01
24	mutexS	2	28	26	2	0.44	0.04	0.01	0.01	0.01
25	minticketS	1	19	18	1	0.31	0.01	0.01	0.01	0.01
26	notsameS	2	28	26	2	0.14	0.02	0.01	0.01	0.01

Heuristics are fundamental

# LEAP: Experimental Results

	formula	#solved vc		Brute time(s.)	Heurist. time(s.)	DP time(s.)		LEAP time(s.)		
		idx	#vc			pos	dp		slowest	average
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2	order	1	121	62	59	998.35	1.12	0.03	0.01	0.47
3	lock	1	121	76	45	778.15	0.47	0.02	0.01	0.18
4	next	1	121	60	61	$\infty$	2.11	0.61	0.01	0.59
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15	next <sub>3</sub>	0	84	65	19	$\infty$	0.67	0.09	0.01	0.20
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18	region	0	1583	1527	56	$\infty$	44.28	22.66	0.54	1.35
19	next	0	1899	1869	30	$\infty$	3.19	0.32	0.02	1.59
20	order	0	2531	2474	57	$\infty$	11.18	9.85	0.24	6.75
21	mutex	2	28	26	2	0.32	0	0	0	0.01
22	minticket	1	19	18	1	0.04	0	0	0	0.01
23	notsame	2	28	26	2	0.13	0.05	0.01	0.01	0.01
24	mutexS	2	28	26	2	0.44	0.04	0.01	0.01	0.01
25	minticketS	1	19	18	1	0.31	0.01	0.01	0.01	0.01
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**LEAP analysis time remains insignificant**



# LEAP: Experimental Results

	formula	#solved vc		Brute time(s.)	Heurist. time(s.)	DP time(s.)		LEAP time(s.)		
		idx	#vc			pos	dp		slowest	average
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3	lock	1	121	76	45	778.15	0.47	0.02	0.01	0.18
4	next	1	121	60	61	$\infty$	2.11	0.61	0.01	0.59
5	region	1						18.17	0.18	0.23
6	disj	2						0.01	0.01	0.12
7	funSchLinear	1						3.04	0.05	0.08
8	funSchInsert	1	121	93	28	$\infty$	4.15	1.91	0.03	0.08
9	funSchRemove	1	121	93	28	$\infty$	5.40	2.60	0.04	0.10
10	funSearch	1	208	198	10	$\infty$	3.54	1.57	0.01	0.34
11	funInsert	1	208	200	8	$\infty$	0.50	0.01	0.01	0.22
12	funRemove	1	208	200	8	$\infty$	1.41	0.95	0.01	0.24
13	skiplist <sub>3</sub>	0	154	92	62	$\infty$	1221.97	776.45	15.27	0.45
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19	next	0	1899	1869	30	$\infty$	3.19	0.32	0.02	1.59
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21	mutex	2	28	26	2	0.32	0.01	0.01	0.01	0.01
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25	minticketS	1	19	18	1	0.31	0.01	0.01	0.01	0.01
26	notsameS	2	28	26	2	0.14	0.02	0.01	0.01	0.01

Decision procedures perform well...  
but still room for improvements

# LEAP: Future Directions and Ideas

Program



Program Parser

Transition System Generator

VC Generator

Formula Parser

Decision Procedures

Pos Skiplists Lists Num

LEAP

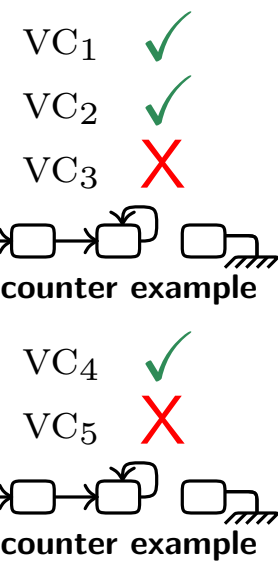
Yices Z3 CVC4

$S_1$

$S_2$

$S_3$

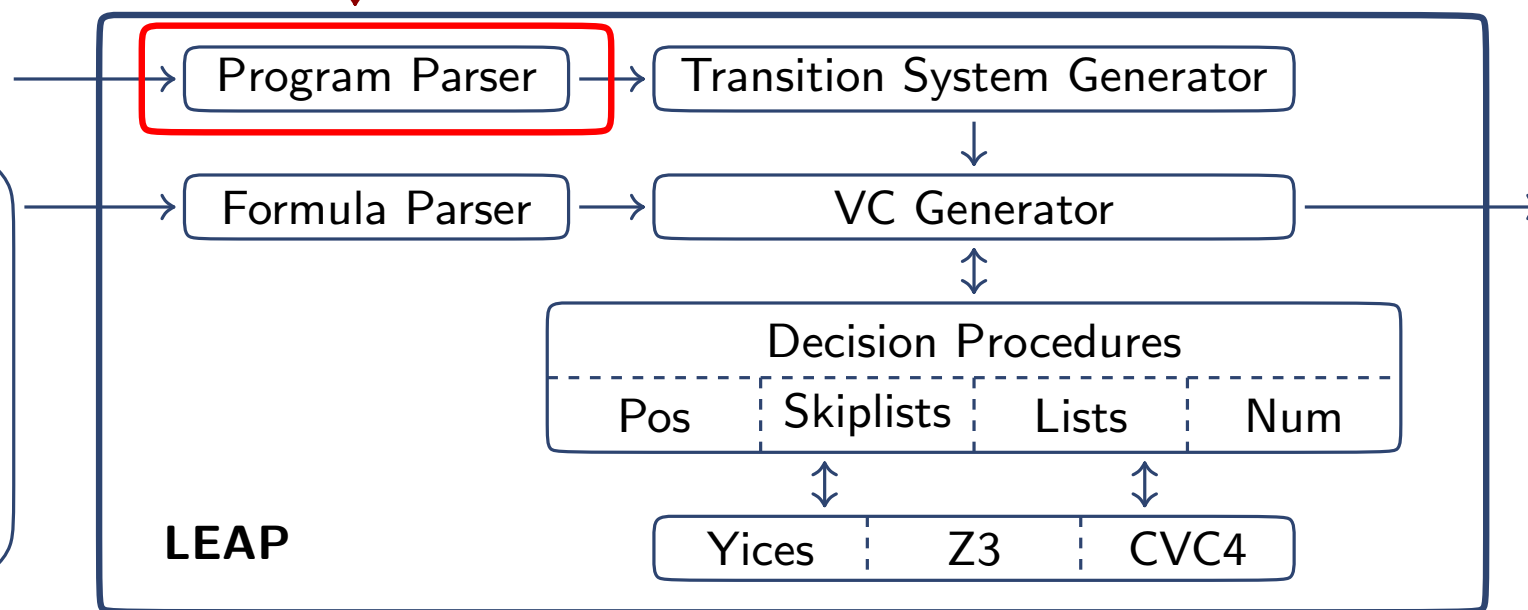
Specs



# LEAP: Future Directions and Ideas

Adapt parser for C,  
JAVA,...  
Use CIL/Frama-C  
as front-end

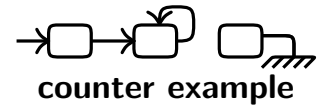
Program



VC<sub>1</sub> ✓

VC<sub>2</sub> ✓

VC<sub>3</sub> ✗



counter example

VC<sub>4</sub> ✓

VC<sub>5</sub> ✗



counter example

Specs

# LEAP: Future Directions and Ideas

Adapt parser for C,  
JAVA,...  
Use CIL/Frama-C  
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Use generated info  
for specs refinement

Program



Program Parser

Transition System Generator

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Decision Procedures

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CVC4

LEAP

VC<sub>1</sub> ✓

VC<sub>2</sub> ✓

VC<sub>3</sub> ✗



counter example

VC<sub>4</sub> ✓

VC<sub>5</sub> ✗



counter example

S<sub>1</sub>

S<sub>2</sub>

S<sub>3</sub>

Specs

# LEAP: Future Directions and Ideas

Adapt parser for C,  
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Use generated info  
for specs refinement

Implement  
liveness

Program



Program Parser

Transition System Generator

$S_1$

Formula Parser

VC Generator

$S_2$

Decision Procedures

Pos

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Lists

Num

$S_3$

LEAP

Yices

Z3

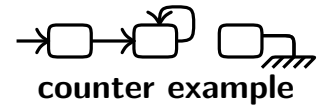
CVC4

Specs

VC<sub>1</sub> ✓

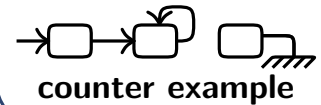
VC<sub>2</sub> ✓

VC<sub>3</sub> ✗



VC<sub>4</sub> ✓

VC<sub>5</sub> ✗



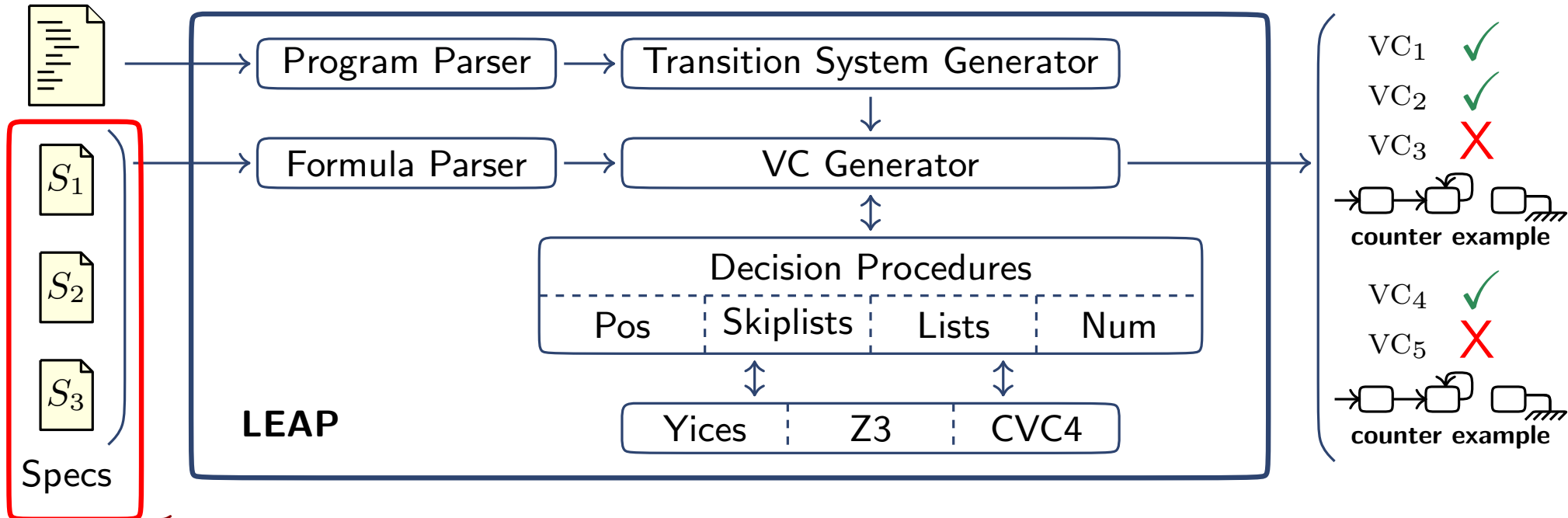
# LEAP: Future Directions and Ideas

Adapt parser for C,  
JAVA,...  
Use CIL/Frama-C  
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Implement  
liveness

Program



Adaptation of  
abstract-interpretation  
invariant generators

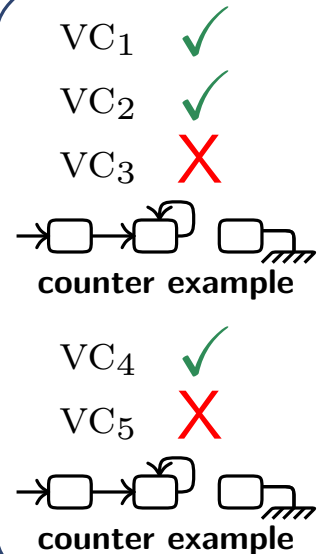
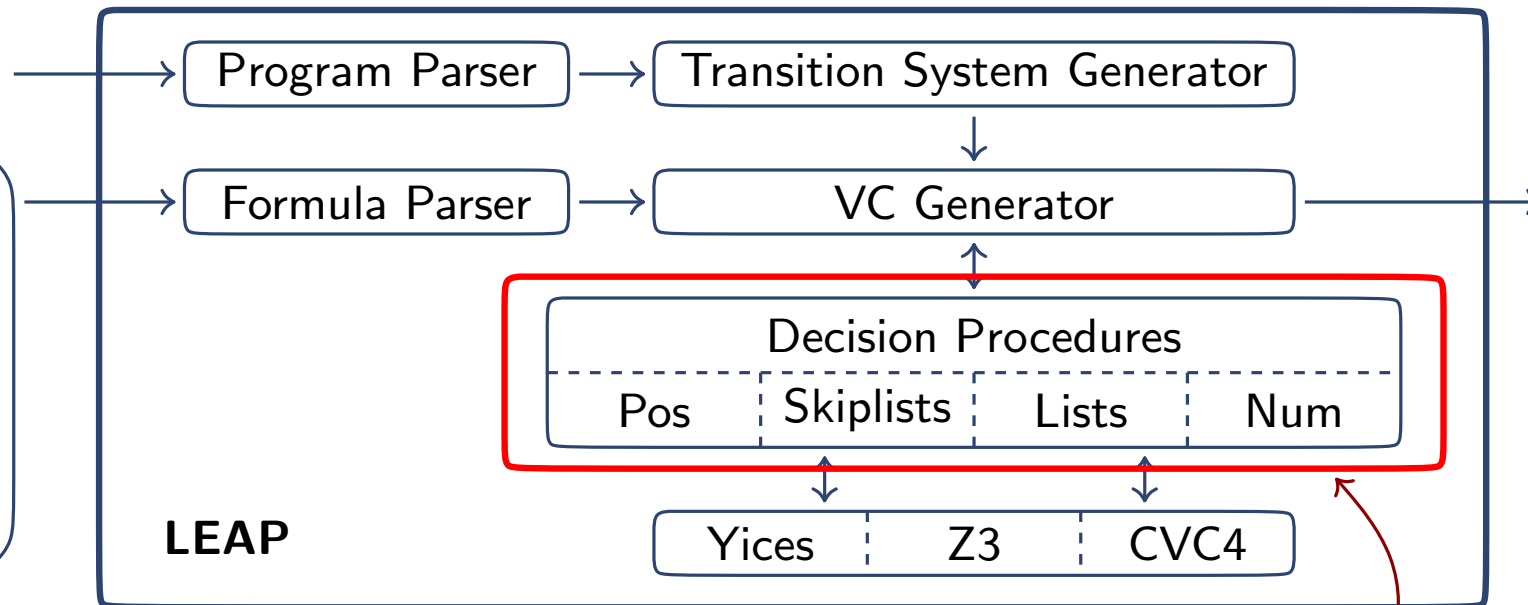
# LEAP: Future Directions and Ideas

Adapt parser for C,  
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Use CIL/Frama-C  
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Use generated info  
for specs refinement

Implement  
liveness

Program



Specs

Adaptation of  
abstract-interpretation  
invariant generators

More decision procedures:  
double-linked lists,  
hashmaps,...

# Conclusions

- ▶ **Deductive** verification tool for **concurrent datatypes**...
- ▶ ... using specialized **decision procedures**
- ▶ Aiming the verification of **parametrized symmetric systems**
- ▶ **Safety** fully implemented, **liveness** ongoing work

**LEAP** and examples **available online** at

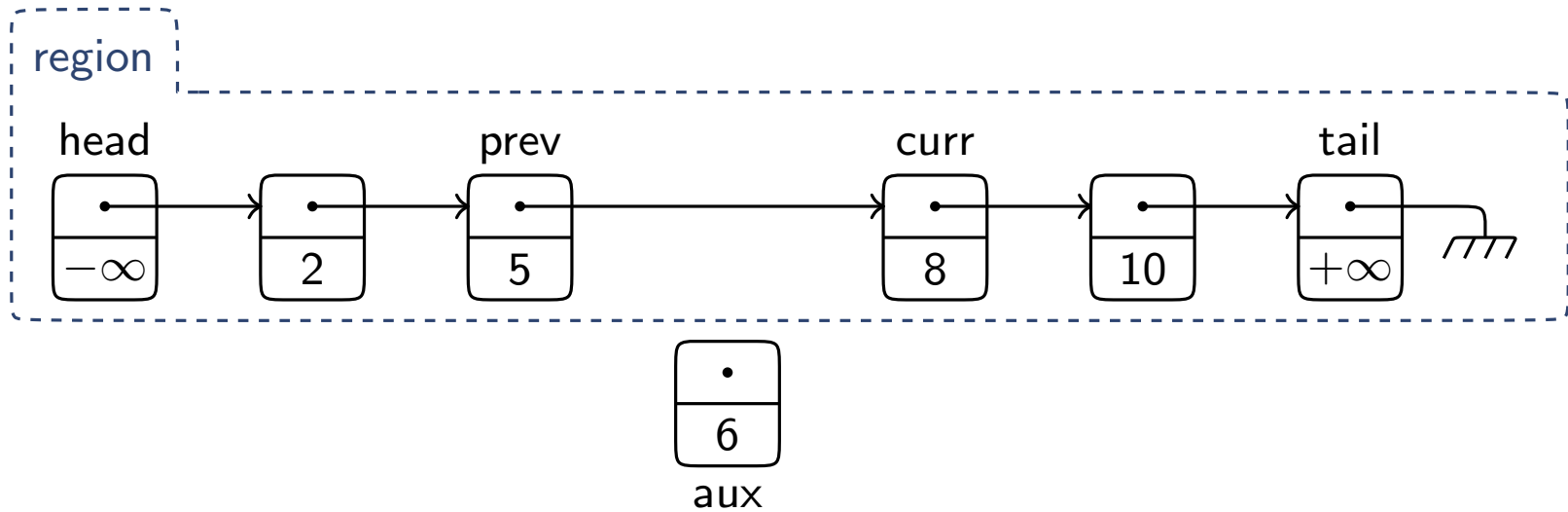
`software.imdea.org/leap`

(demo on demand)



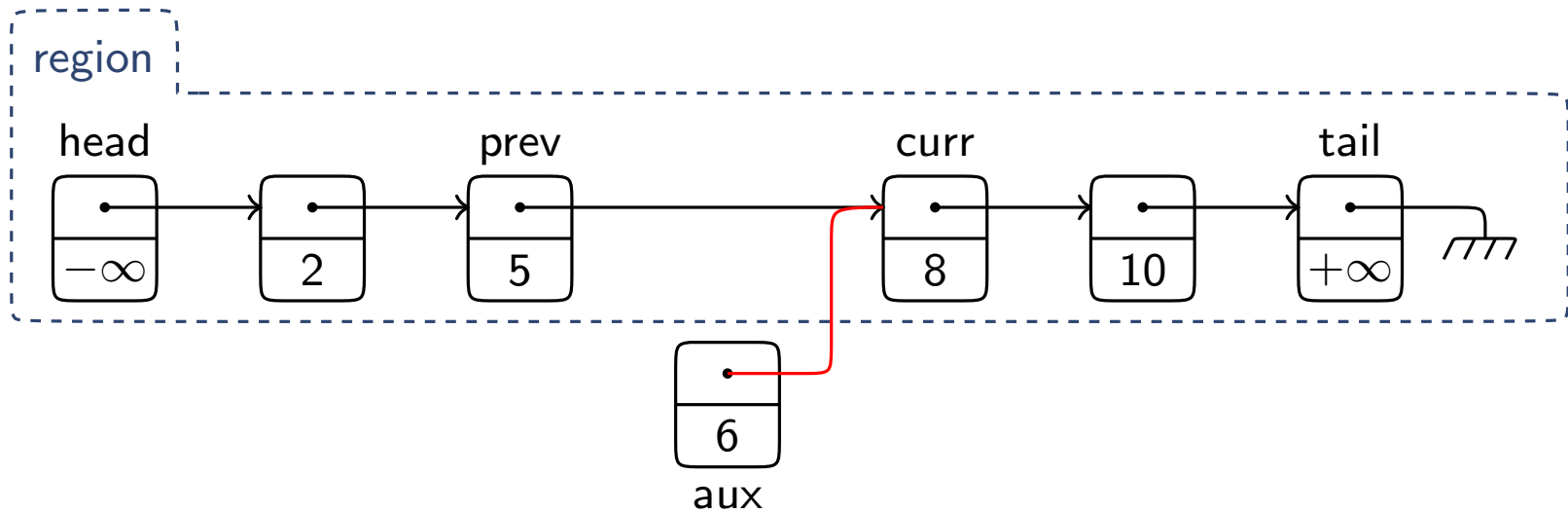
# Demo

- ▶ **List preservation** concurrent lock-coupling single-linked lists



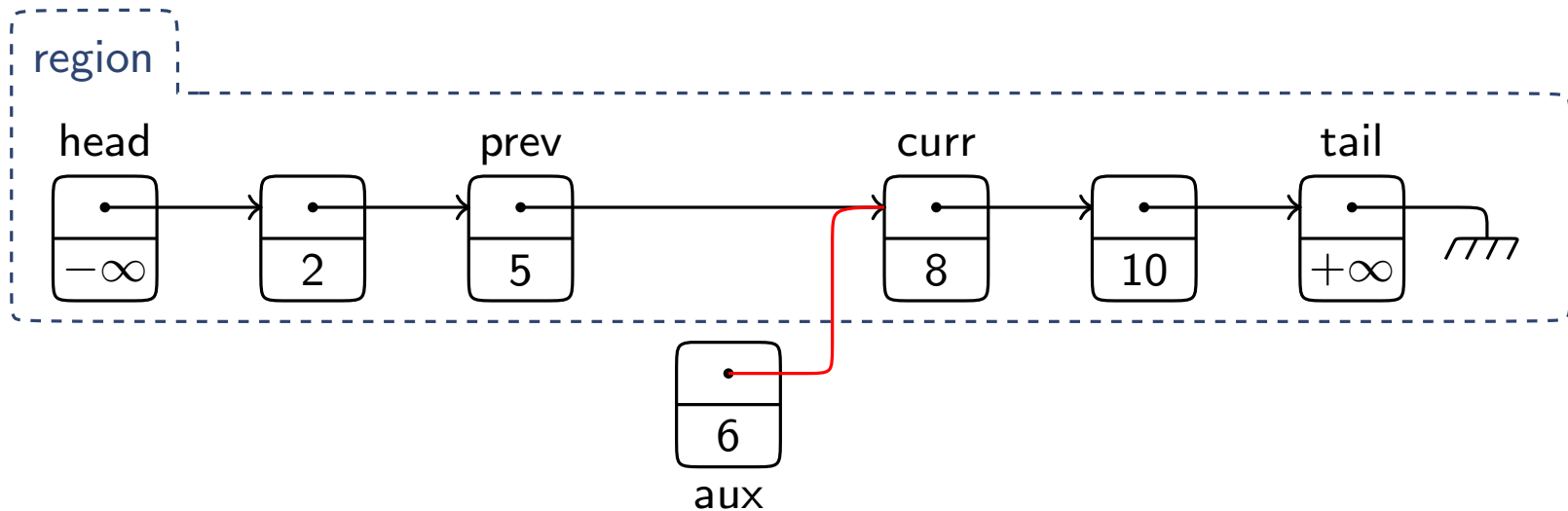
# Demo

- ▶ **List preservation** concurrent lock-coupling single-linked lists
- ▶ Transition 34:  $\text{aux} \rightarrow \text{next} := \text{curr}$

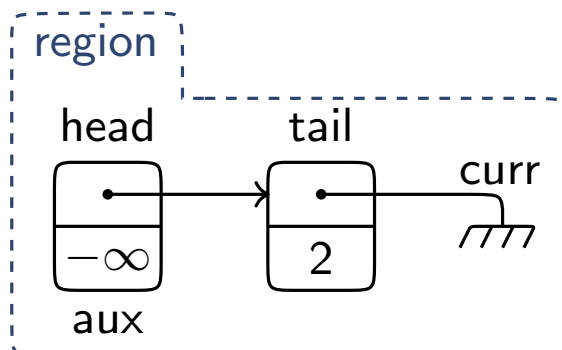


# Demo

- ▶ **List preservation** concurrent lock-coupling single-linked lists
- ▶ Transition 34:  $\text{aux} \rightarrow \text{next} := \text{curr}$

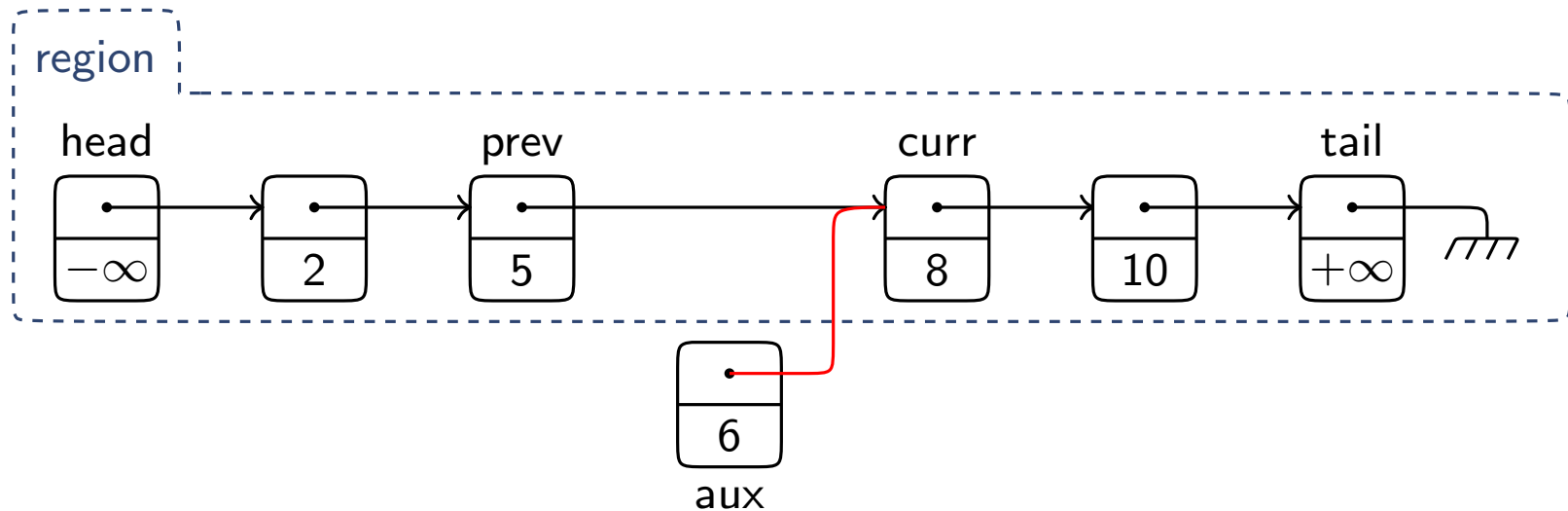


- ▶ **Counter example**



# Demo

- ▶ **List preservation** concurrent lock-coupling single-linked lists
- ▶ Transition 34:  $\text{aux} \rightarrow \text{next} := \text{curr}$



- ▶ **Counter example**

